
ν -Nucleus Scattering Yields: Interplay of Neutrino Flux, Cross sections and Nuclear Effects

Jorge G. Morfín – Fermilab
MINER ν A Collaboration Meeting – February 2013

ν – H / D Scattering

Life was simpler when our targets were **nucleons** as opposed to **nuclei**.

$$\sigma = \frac{N_{obs} - N_{bgd}}{\Phi * N_{targets} * \epsilon}$$

Number of neutrinos (flux) $\rightarrow \Phi$

Number of nuclei $\rightarrow N_{targets}$

Reconstruction efficiency $\leftarrow \epsilon$

Neutrino Nucleus Scattering

What do we observe in our detectors?

- ◆ The events we observe in our detectors are convolutions of:
$$Y_{\text{c-like}}(E) \propto \phi(E' \geq E) \otimes \sigma_{\text{c,d,e.}}(E' \geq E) \otimes \text{Nuc}_{\text{c,d,e.} \rightarrow \text{c}}(E' \geq E)$$
- ◆ $Y_{\text{c-like}}(E)$ is the event energy and channel / topology of the event observed in the detector. It is called c-like since it appears to be channel c but may not have been channel c at interaction.
- ◆ That is the topology measured in the detector is what we observe in the detector and not necessarily what was produced at the initial interaction.
- ◆ The energy E is not given by knowing the E of the incoming particle as in charged particle scattering, but is the sum of energies coming out of the nucleus and measured in the detector.

Neutrino Nucleus Scattering

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 - ◆ $\phi(E)$ is the energy dependent neutrino flux that enters the detector.
 - ◆ We can, with considerable effort, estimate the incoming neutrino energy distribution to $\leq 10\%$ absolute and $\leq 7\%$ **energy-bin to energy-bin accuracy** with sophisticated Monte Carlos that depend on knowledge of the hadron production spectra off the target and careful modeling of the subsequent beam components.

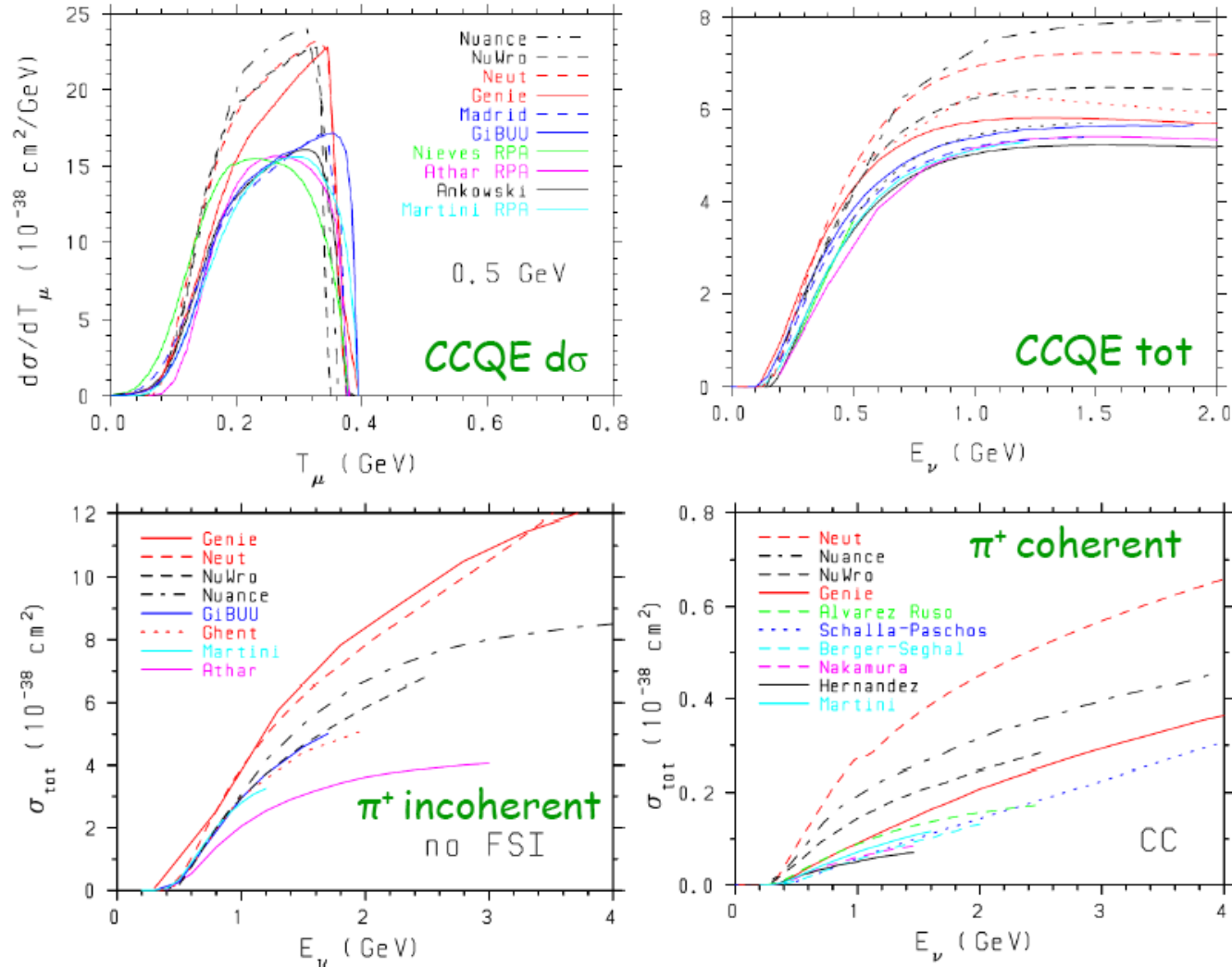
Neutrino Nucleus Scattering

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 - ◆ $\sigma_{\text{c,d,e..}}(E' \geq E)$ is the measured or the Monte Carlo (model) energy dependent neutrino cross section off a **nucleon within a nucleus**.
 - ◆ Form factors are modified within a nucleus compared to a nucleon.
 - ◆ Analogous to the difference between PDFs and nuclear NPDFs
 - ◆ The width of the Δ changes within a nucleus.
 - ◆ A bit tricky to measure without the next convoluted quantity....

Range of Existing Model (MC) Predictions off C

NuInt09 – Steve Dytman



Jorge G. Morfín - Fermilab

Neutrino Nucleus Scattering

What do we observe in our detectors?

- ◆ The events we observe in our detectors are convolutions of:

$$Y_{c\text{-like}}(E) \propto \phi(E' \geq E) \otimes \sigma_{c,d,e..}(E' \geq E) \otimes \text{Nuc}_{c,d,e.. \rightarrow c}(E' \geq E)$$

- ◆ **$\text{Nuc}_{c,d,e.. \rightarrow c}(E' \geq E)$ – Nuclear Effects**

- ◆ In contemporary neutrino experiments the interactions do not occur on a free nucleon but rather nucleon(s) within a nucleus and there are many nuclear effects that have to be considered.
- ◆ In general the interaction of a neutrino with energy E' creating initial channel $d,e...$ can appear in our detector as energy E and channel c
- ◆ **Nuclear Effects** – a migration matrix that mixes produced/observed channels and energy.

What are these Nuclear Effects $\text{Nuc}_{c,d,e.. \rightarrow c} (E' \geq E)$ in Neutrino Nucleus Interactions?

- ◆ Target nucleon in motion – classical Fermi gas model or the superior spectral functions (Benhar et al.)
- ◆ Certain reactions prohibited - Pauli suppression
- ◆ Meson exchange currents: multi-nucleon initial states
- ◆ Form factors and resonance widths are modified within the nuclear environment. (Butkevich / Kulagin, Tsushima et al.)
- ◆ Produced topologies are modified by final-state interactions modifying topologies and possibly reducing **detected** energy.
 - ▼ Convolution of $\delta\sigma(n\pi)$ (x) formation zone uncertainties (x) π -charge-exchange/absorption (nuclear density uncertainties)
- ◆ Cross sections and structure functions are modified and parton distribution functions within a nucleus are different than in an isolated nucleon. **Important for DIS AND Transition region events!**

What do we observe in our detectors?

- ◆ The events we observe in our detectors are convolutions of:

$$Y_{\text{c-like}}(E) \propto \phi(E' \geq E) \otimes \sigma_{\text{c,d,e..}}(E' \geq E) \otimes \text{Nuc}_{\text{c,d,e..} \rightarrow \text{c}}(E' \geq E)$$

effective $\sigma_{\text{c}}^{\text{A}}(E)$

- ◆ Experimentally, the last two terms convoluting the initial nucleon (within a nucleus) cross section and nuclear effects are combined into an effective cross section $\sigma_{\text{c}}^{\text{A}}(E)$ and we now have:

$$\sigma_{\text{c-like}}^{\text{A}}(E) \propto Y_{\text{c-like}}^{\text{A}}(E, \text{Nuc}(E' \geq E)) / \phi(E' \geq E)$$

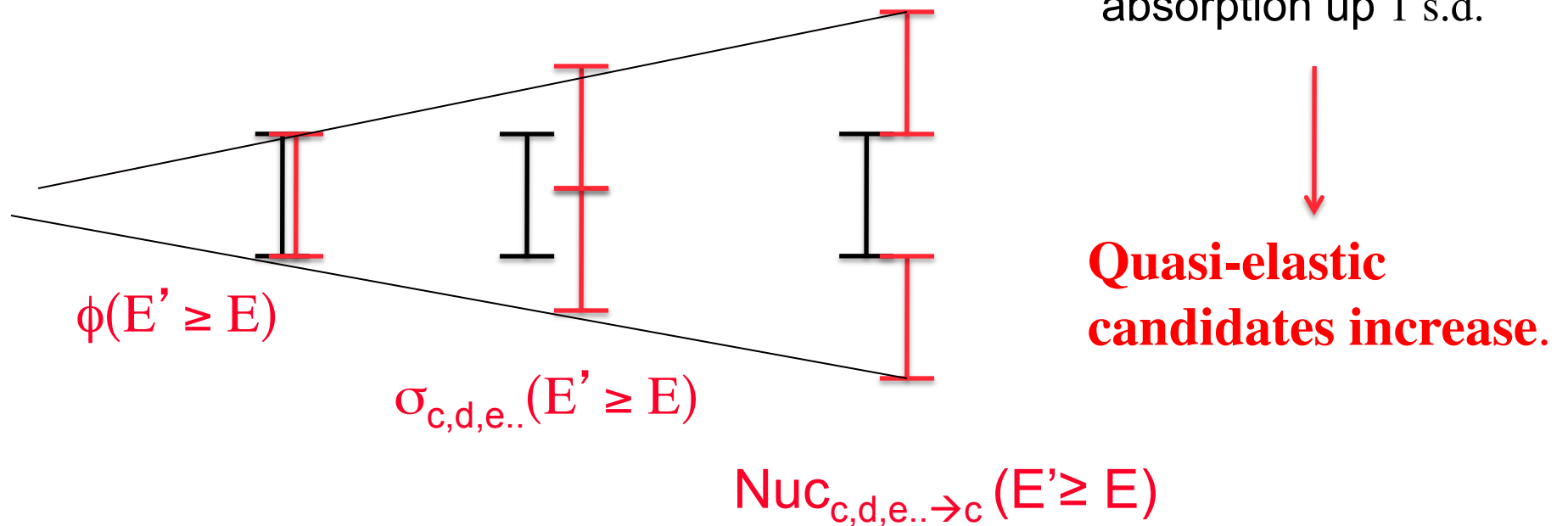
- ◆ Note that the **effective cross section $\sigma_{\text{c}}^{\text{A}}(E)$ measured depends on the incoming neutrino energy spectrum and the involved nuclear effects that populate the yield $Y_{\text{c}}^{\text{A}}(E)$.**
- ◆ This implies that, for example, the effective $\sigma_{\pi^0}^{\text{C}}(1 \text{ GeV})$ measured in the MiniBooNE Booster beam **will be different** than the same effective $\sigma_{\pi^0}^{\text{C}}(1 \text{ GeV})$ observed by MINERvA in the higher energy NuMI beam due to, for example, more feed down from multi-pi events via pion absorption in the NuMI beam.

Systematics

Flux for $E > E_{\Delta}^{\text{thresh}}$
up 1 s.d.

Cross section for Δ
production up 1 s.d.

Probability for π
absorption up 1 s.d.



Significant Implications for Oscillation Experiments

- ◆ Can not simply plug in effective $\sigma_{\pi 0}^A$ from experiments in a significantly different beam.
- ◆ In a two-detector oscillation experiment the neutrino flux entering the far detector is altered from the neutrino flux at the near detector due to oscillations.
- ◆ The $\sigma_c^A(E)$ effective that should be applied to expectations (Monte Carlo) at the far detector is NOT the same as that which we would measure at the near detector. **However, the near detector results give us an excellent starting point for calculating the difference.**
- ◆ **The convoluted $\phi(E' \geq E)$ \otimes $\sigma(E)$ \otimes Nuc($E' \geq E$) systematics need to be correctly incorporated in determining the systematics of oscillation parameter measurements.**

What can we do to study this?

- ◆ Lots of CPU to model the effect....
- ◆ Study same “-like” channels in the LE and ME beam
- ◆ Reweight the LE near detector beam spectra to the MINOS far detector measured oscillated spectra. What do we see for “QuasiElastic – like “ events.
- ◆

Summary and Conclusions

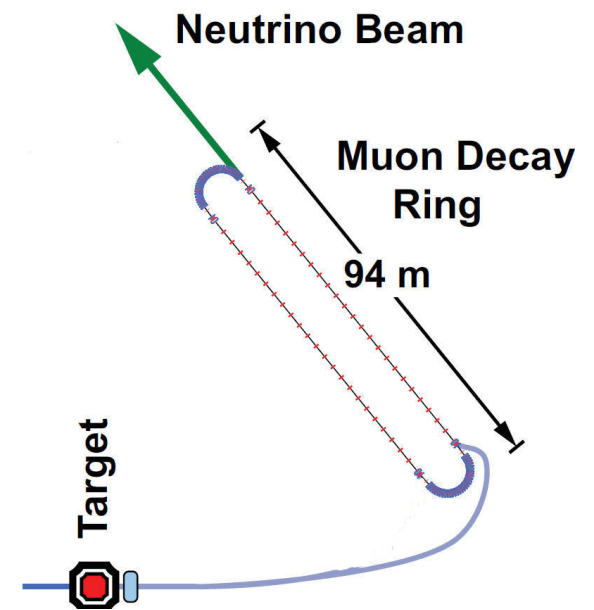
- ◆ Nuclear effects, present in the data of all contemporary neutrino oscillation experiments, **mixes channels and changes energy between produced and final states (observed)**.
- ◆ Observed results for a specific channel from one detector does not transfer to another detector unless they are using the same neutrino beam. **What is a “standard candle”?**
- ◆ Need to study these effects on a variety of nuclear targets and with a variety of incoming neutrino energy distributions. **MINERvA in the LE and ME beams!**
- ◆ To untangle these effects, a significant step forward would be a high-statistics neutrino-hydrogen /deuterium experiment.
- ◆ Best would be in a neutrino beam with a flux that we know to $\approx 1\%$.

Backup

Can we Actually MEASURE these Differences in the 0.5 – 4 GeV region

ν STORM Neutrinos from Stored Muons

- ◆ High-Precision ν interaction physics program.
- ▼ The ν STORM beam will provide a very well-known ($\delta \phi(E) \approx 1\%$) beam of ν and $\bar{\nu}$.
 - ▼ ν_e and $\bar{\nu}_e$ cross-section measurements.
 - ▼ ν_μ and $\bar{\nu}_\mu$ cross-section measurements
- ◆ Address the large Δm^2 oscillation regime, make major contribution to the study of sterile neutrinos
 - ▼ Either allow for precision study (in many channels), if they exist in this regime.
 - ▼ Or greatly expand the dis-allowed region.
- ◆ Provide a μ decay ring test demonstration and μ beam diagnostics test bed.
- ◆ Provide a precisely understood ν beam for detector studies.
- ◆ **Change the conception of the neutrino factory.**

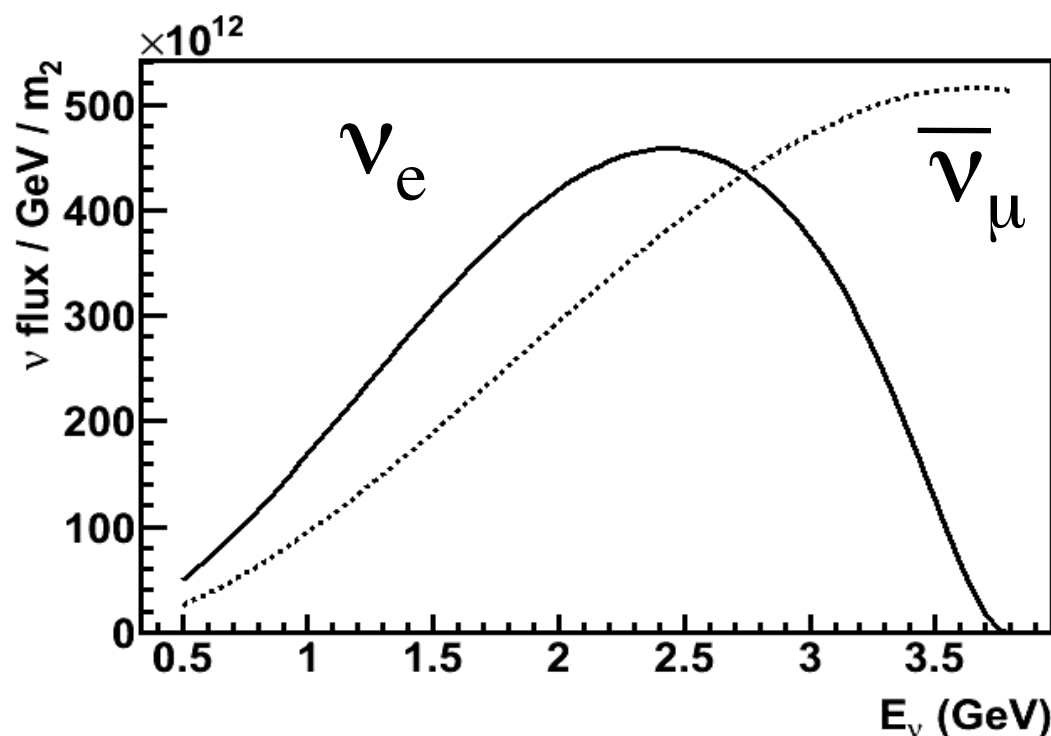


The νSTORM Neutrino Beam

$$\mu^+ \rightarrow \bar{\nu}_\mu + \nu_e + e^+$$

$$\mu^- \rightarrow \nu_\mu + \bar{\nu}_e + e^-$$

- ◆ A high-intensity source of ν_e events for experiments.



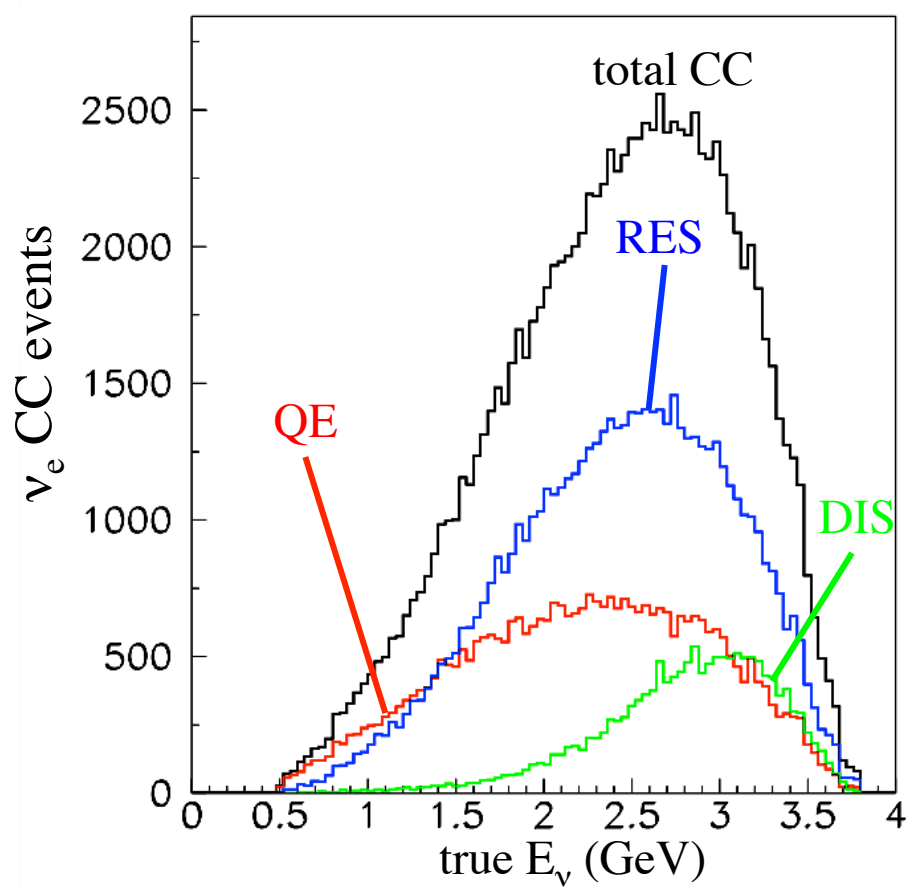
3.8 GeV μ^+ stored, 150m straight, flux at 100m
(thanks to Sam Zeller and Chris Tunnell!)

μ^+		μ^-	
Channel	N_{evts}	Channel	N_{evts}
$\bar{\nu}_\mu$ NC	844,793	$\bar{\nu}_e$ NC	709,576
ν_e NC	1,387,698	ν_μ NC	1,584,003
$\bar{\nu}_\mu$ CC	2,145,632	$\bar{\nu}_e$ CC	1,784,099
ν_e CC	3,960,421	ν_μ CC	4,626,480

event rates per 1E21 POT -
 100 tons at 50m

ν_e Event Fractions in ν STORM

- ◆ ν_e produced by 3.8 GeV μ^+ beam.



**out of the
CC modes:**

* 56%

resonant

* 32% QE

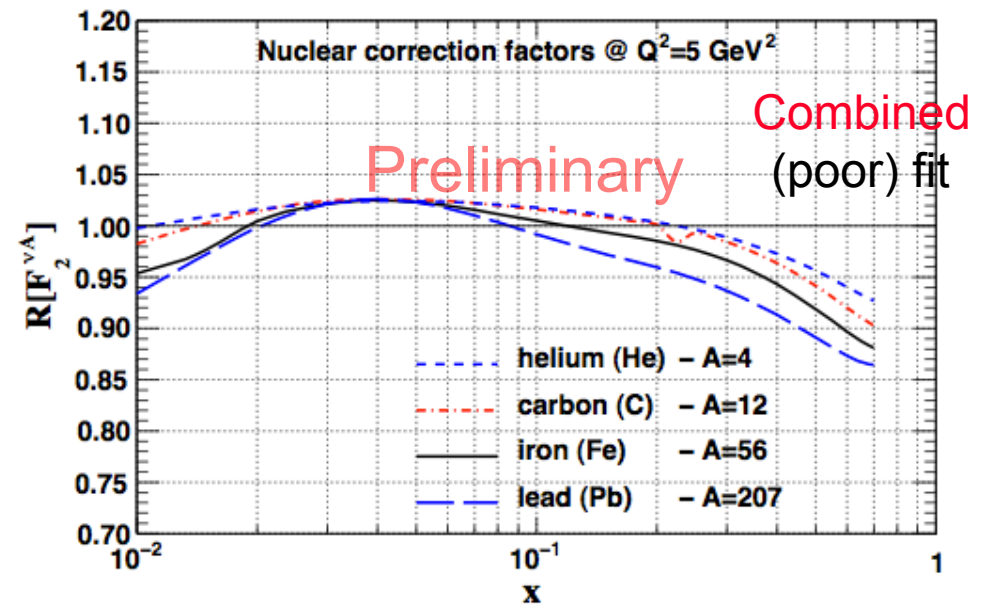
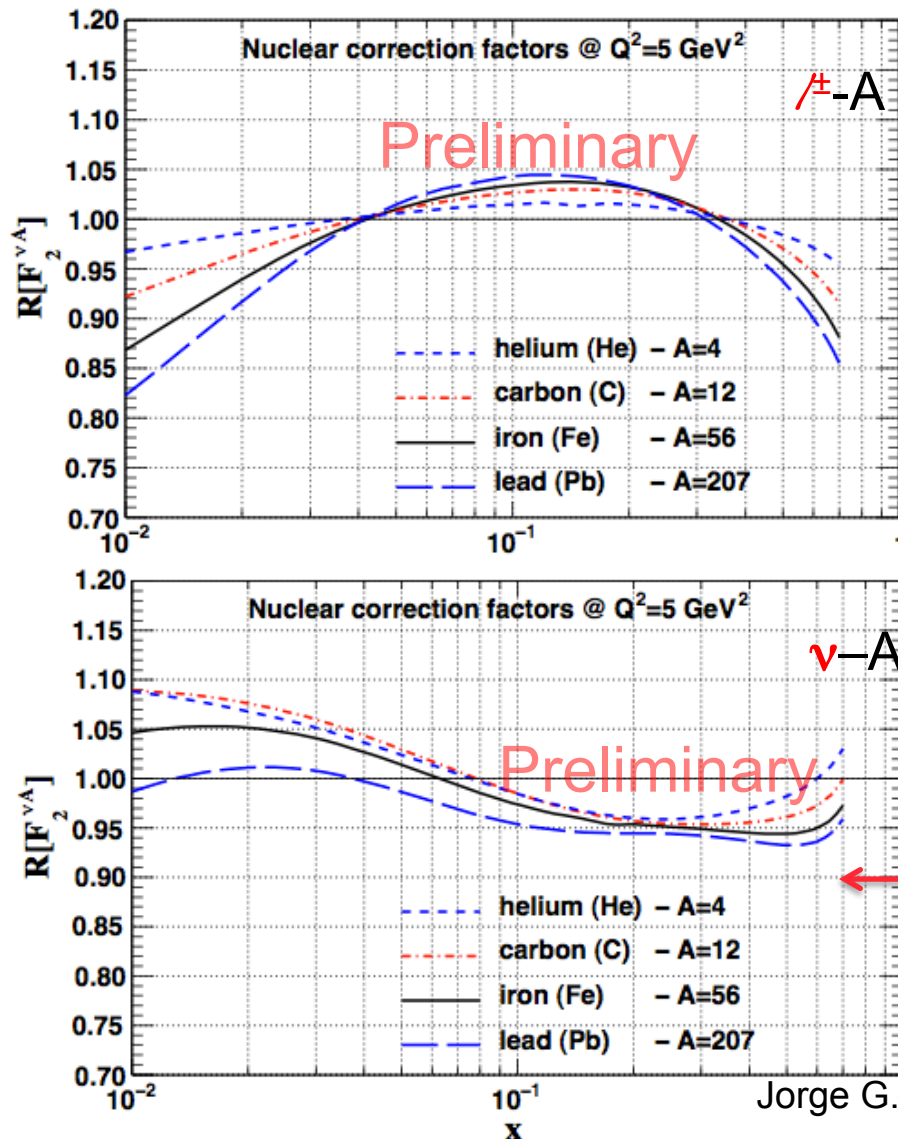
* 12% DIS

- ◆ For $\bar{\nu}_e$ sample, 52% resonant, 40% QE, 8% DIS)

Jorge G. Morfin - Fermilab

What could MINERvA Contribute?

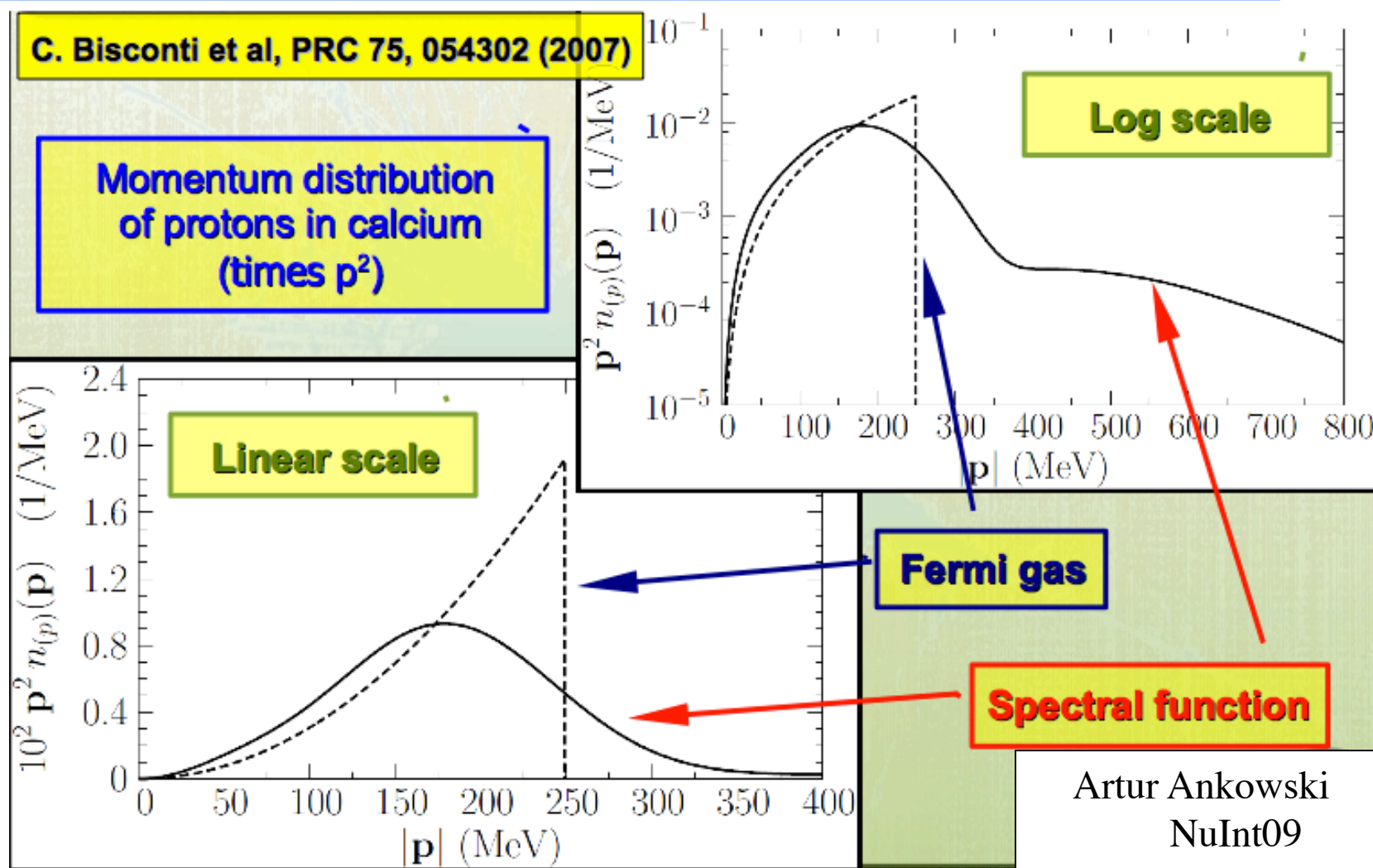
Preliminary Predictions for MINERvA Targets



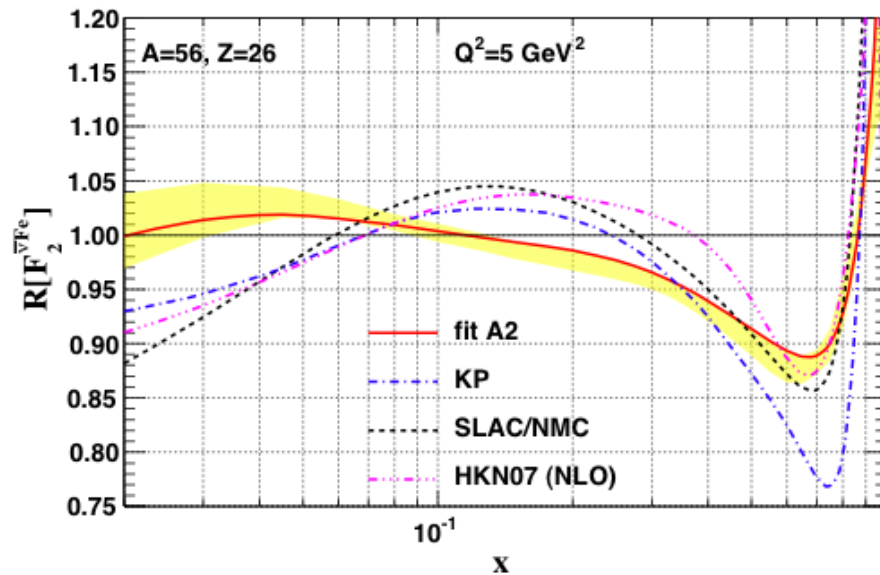
Careful! Based on analysis of NuTeV ν -Fe results and scaled in A as **charged lepton nucleus** scattering results!
(Karol Kovarik – Karlsruhe)

Fermi Gas vs. Spectral Function p Distribution

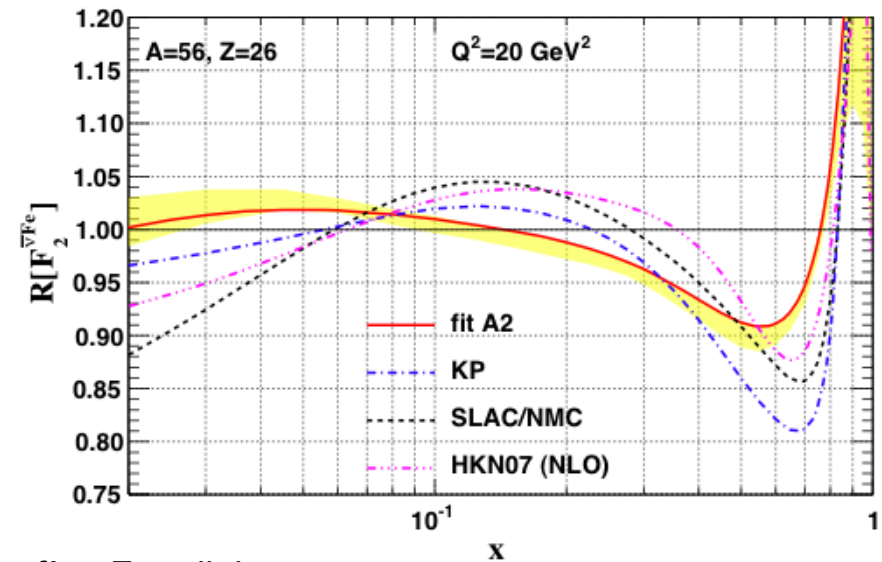
Bodek – Ritchie adds high p tail to FG due to SRC



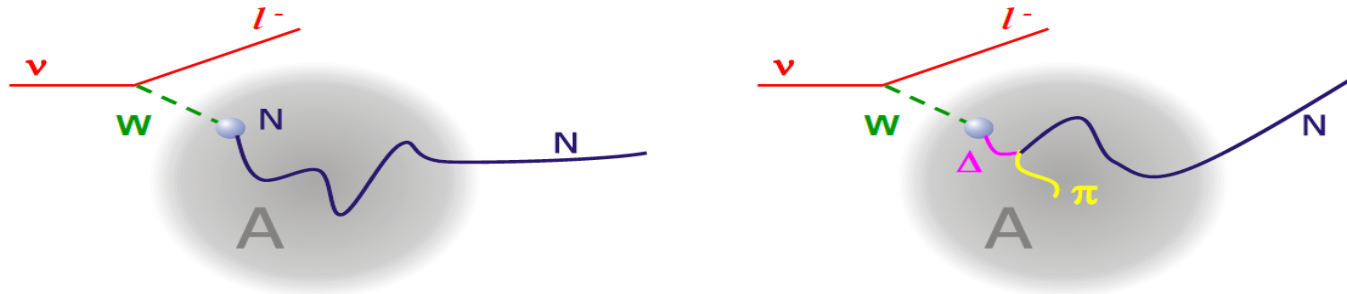
F_2 Structure Function Ratios: $\bar{\nu}$ -Iron



$$\frac{F_2(\nu + \text{Fe})}{F_2(\nu + [n+p])}$$



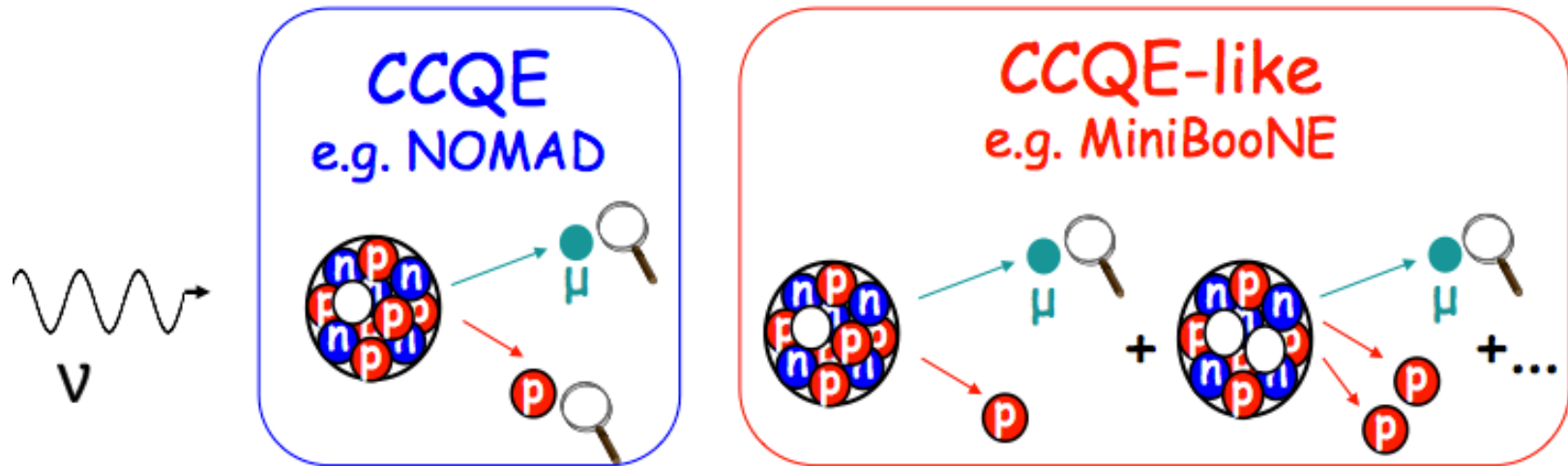
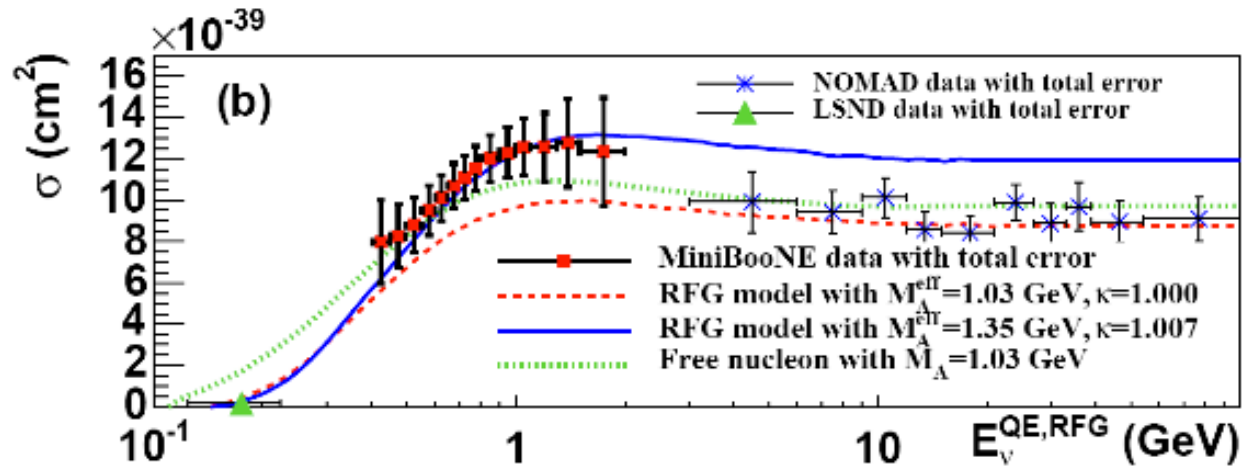
Final State Interactions can mimic a QE event



- ◆ Define a class of events as “**QE-like**” that have the apparent topology but can have been produced as something other than QE.

QE and QE-like events

M.Martini
NuFact09

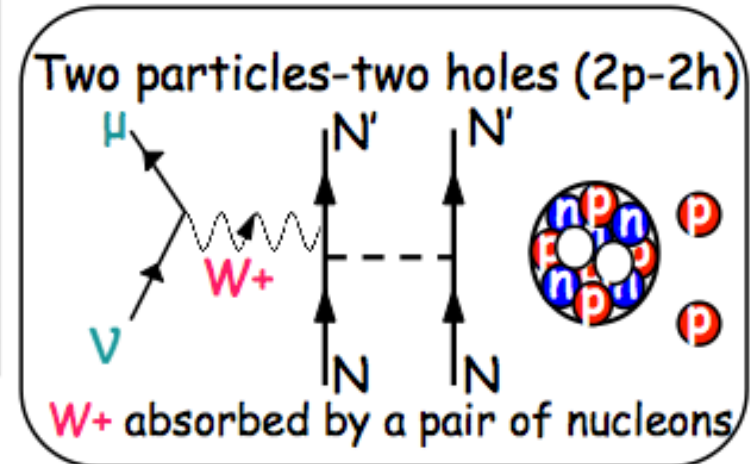
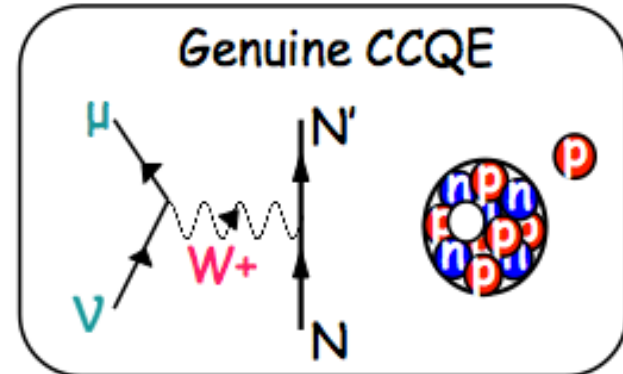
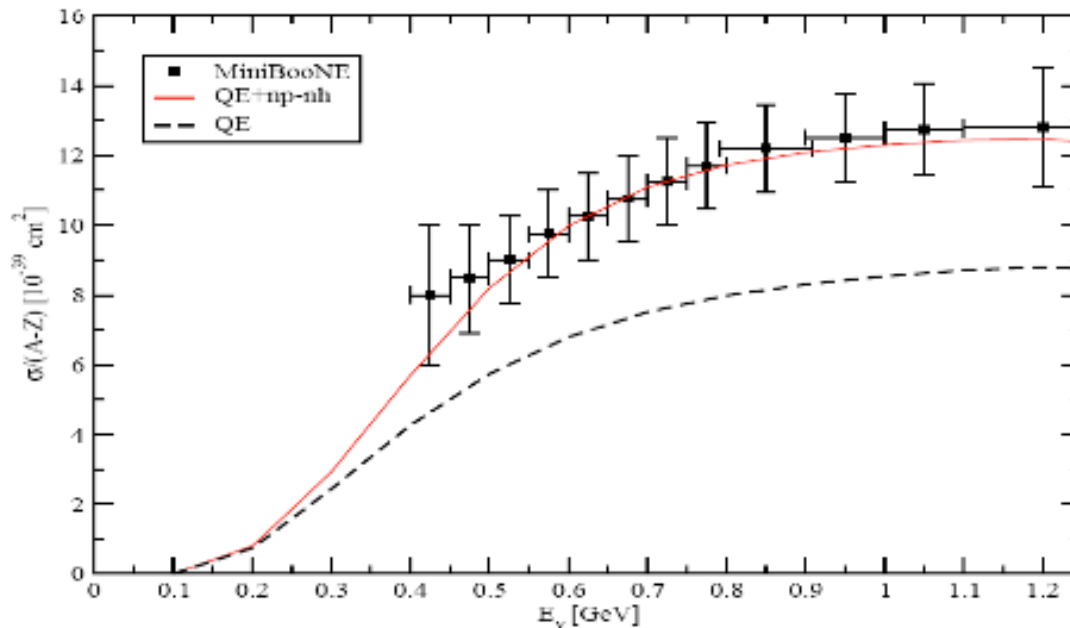


Meson Exchange Currents – 2p2h Effects

CCQE and CCQE-like

energy atomic - energies alternatives

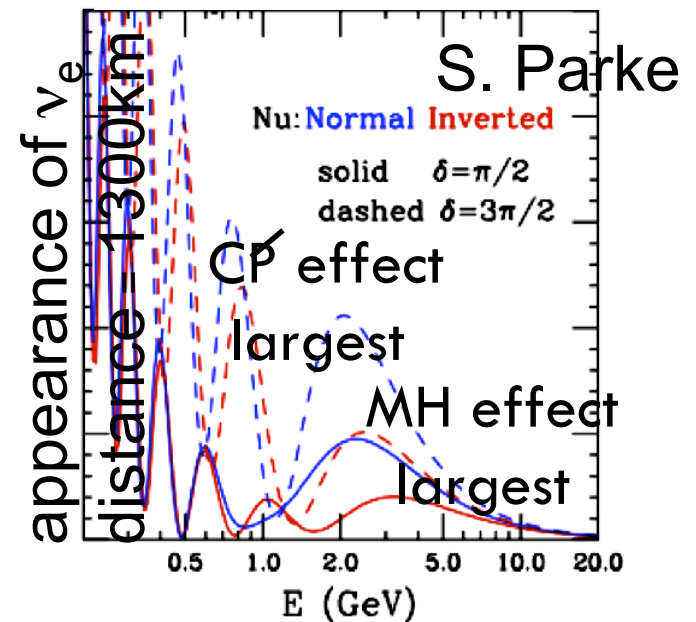
Inclusion of the multinucleon emission channel (np-nh)



M. Martini, M. Ericson, G. Chanfray, J. Marteau Phys. Rev. C 80 065501 (2009)

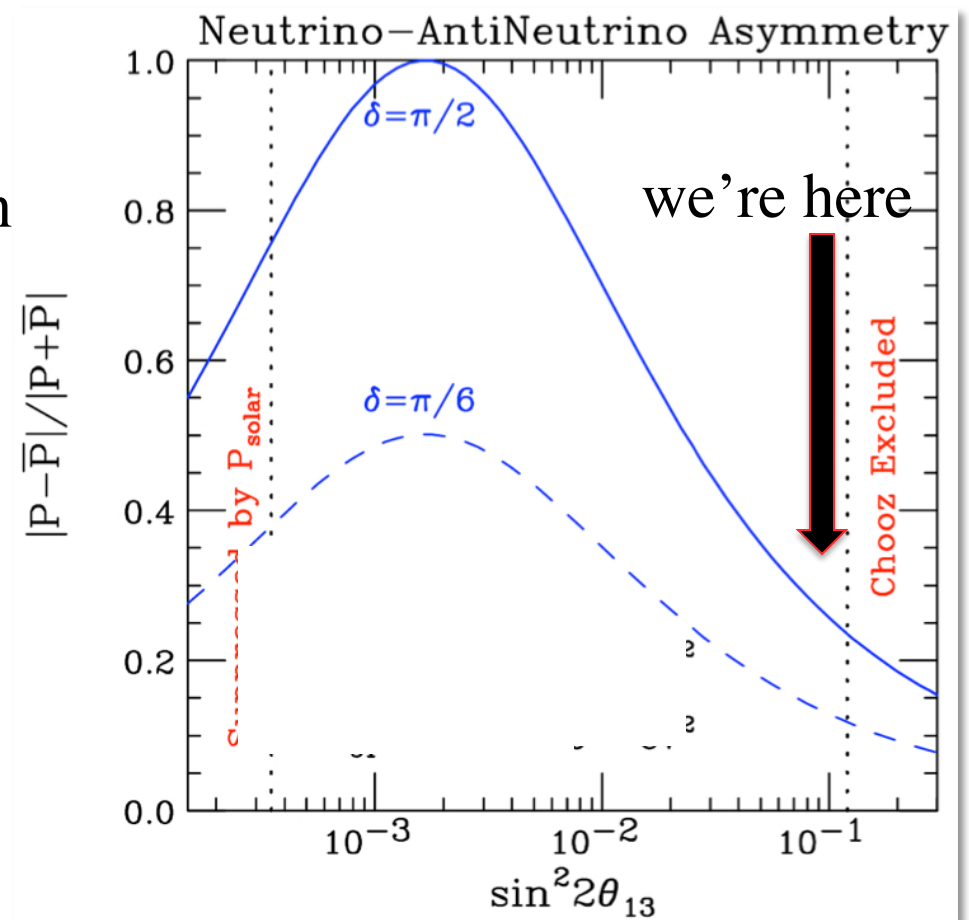
Why are ν_e Cross Sections Important?

- ◆ ν_e A – scattering results are interesting on their own.
- ◆ Recent determination of large θ_{13} has opened up possibilities of
 - ▼ Determining ν mass ordering.
 - ▼ Searching for CP-violation in the ν sector.
- ◆ To be sensitive to these effects, current/near-future long-baseline experiments will be looking for ν_μ to ν_e and $\bar{\nu}_\mu$ to $\bar{\nu}_e$ oscillations over a range of energies.
- ◆ These will no longer be only “counting” experiments but rather will depend on observing distortions in the far detectors neutrino energy spectrum in **both neutrino and anti-neutrino samples**



Why are ν_e and $\bar{\nu}_e$ Cross Sections Important?

- ◆ Large θ_{13} means we could have reasonable statistics.
- ◆ However, as the now-well-known plot at right suggests, the asymmetry between ν and $\bar{\nu}$ will be small and the goal of constraining the range of δ will demand minimal systematic errors.
- ◆ One of these systematics will be our knowledge of ν_e and $\bar{\nu}_e$ cross sections in the relevant energy range.

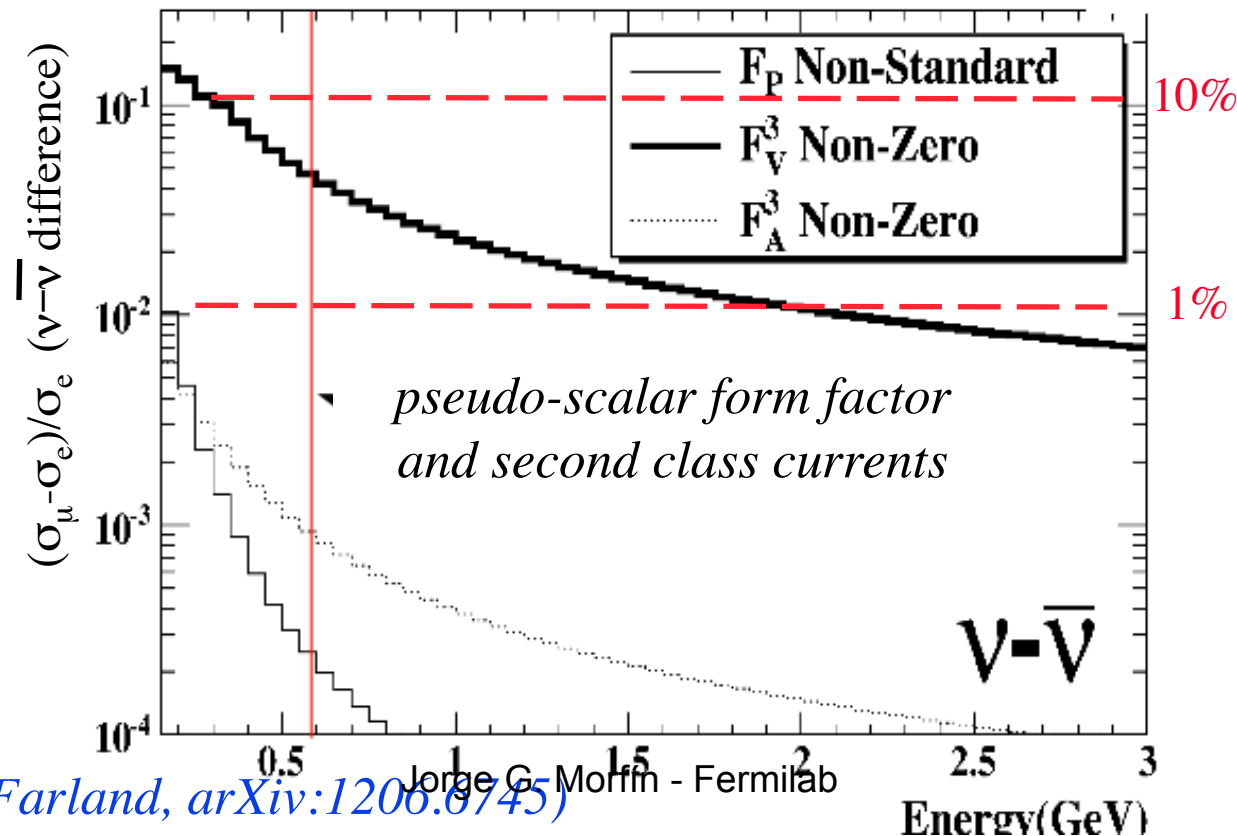


(not including matter effects & backgrounds)
(S. Parke)

What are the Differences $\sigma_{\nu\mu}(E)$ and $\sigma_{\nu e}(E)$? Quasi-elastic Scattering

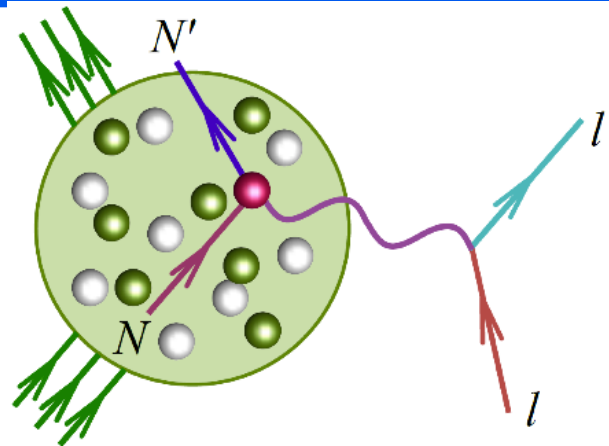
Day-McFarland study: Phys.Rev. D86 (2012) 053003

- ◆ Sources of possible differences: form factor uncertainties entering through lepton mass alterations - much more subtle:
 - ▼ Form factor contributions – both Axial and Pseudoscalar
 - ▼ Second class current contributions to vector and axial-vector form factors
- ◆ Possible contribution to CP uncertainties: effect on the FF could be different for ν and $\bar{\nu}$



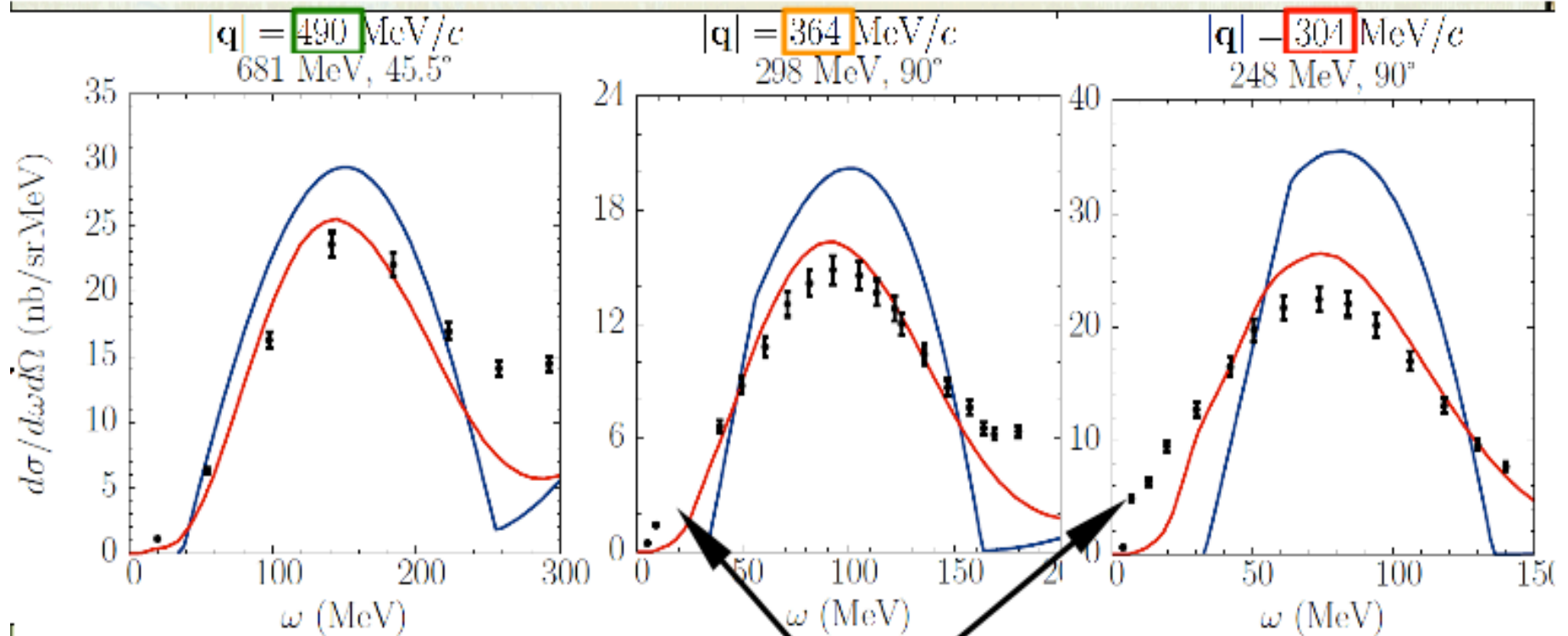
(M. Day, K. McFarland, [arXiv:1206.6745](https://arxiv.org/abs/1206.6745))

Target Nucleon in Motion – Classical Fermi Gas Model or the Superior Spectral Functions



- ◆ Impulse Approximation (IA) – nucleus treated as a collection of independent nucleons – no collective excitations
 - ▼ breaks down as Q decreases with spatial resolution decreasing as $1/Q$
- ◆ In the IA the nucleus is fully described by its spectral function
 - ▼ The spectral function gives the distribution of momenta and energies of the nucleons inside the nucleus
- ◆ The original model to describe this distribution is the Fermi Gas model

Spectral Function Approach Superior – Particularly as Q Decreases



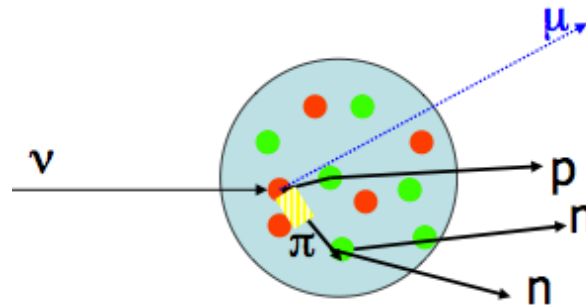
Spectral function

Fermi gas

When $|q| \leq 400$ MeV two- and
few-nucleon contributions appear

Artur Ankowski
NuInt09

Final State Interactions (FSI)

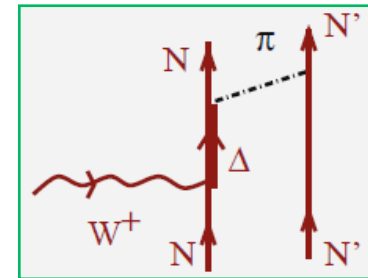
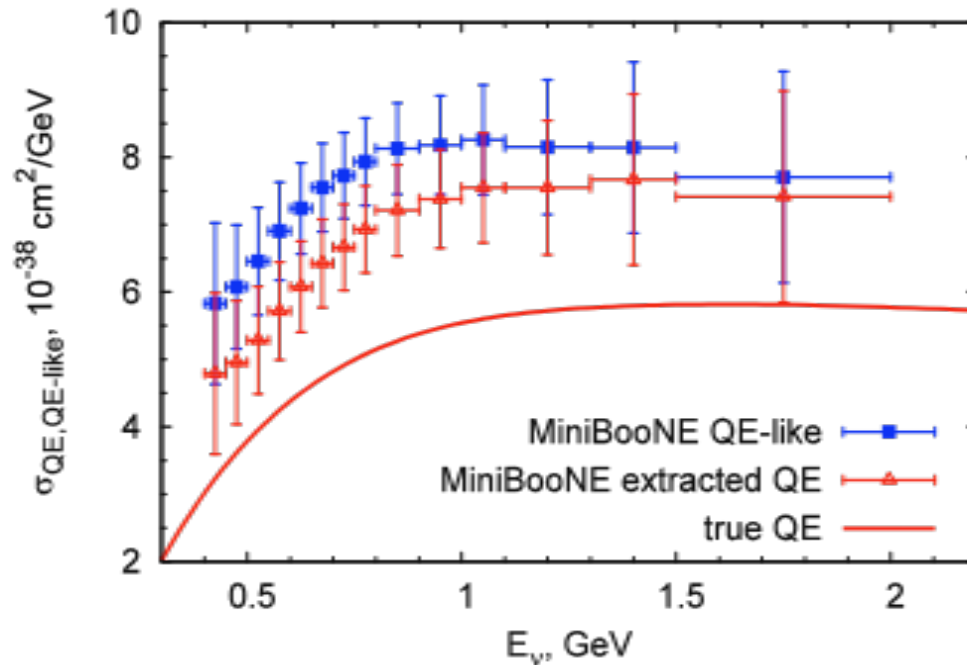


- ◆ Components of the initial hadron shower interact within the nucleus changing the apparent final state configuration and even the detected energy.
- ◆ For example, an initial pion can charge exchange or be absorbed on a pair of nucleons and an initial nucleon can scatter producing a pion

Example numbers	Final μ p	Final μ p π
Initial μ p	90%	10%
Initial μ p π	25%	75%

Attempt to Remove Resonance Background

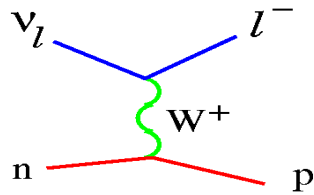
MiniBooNE Experiment example



Event generator – a particular model - is used to remove QE-like background (pion absorption) from QE-like Xsect (blue) yielding an extracted QE Xsect (red) → large pion absorption model dependence of QE result.

Nuclear Effects can Change the Energy Reconstruction for “QE” Events

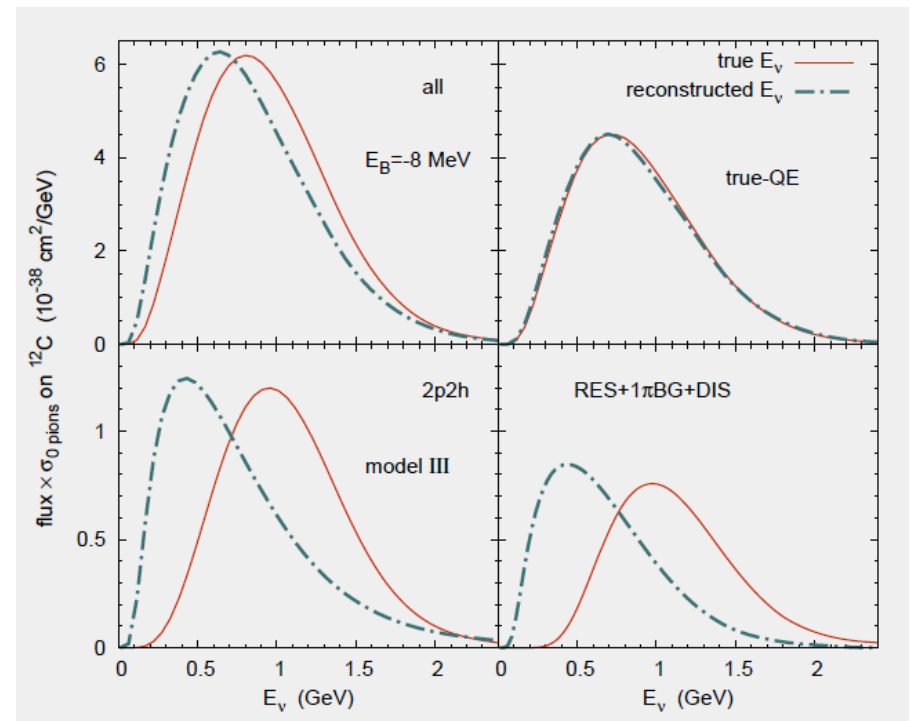
- In pure QE scattering on nucleon at rest, the outgoing lepton can determine the neutrino energy:



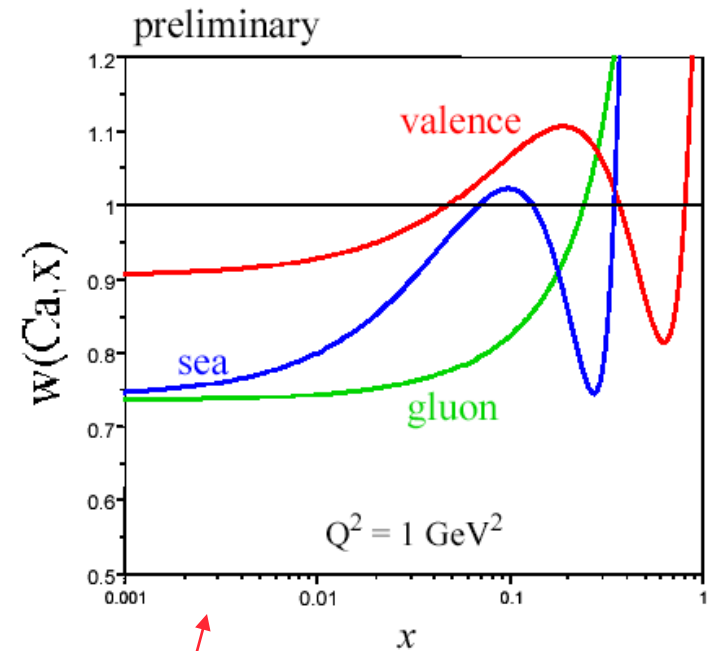
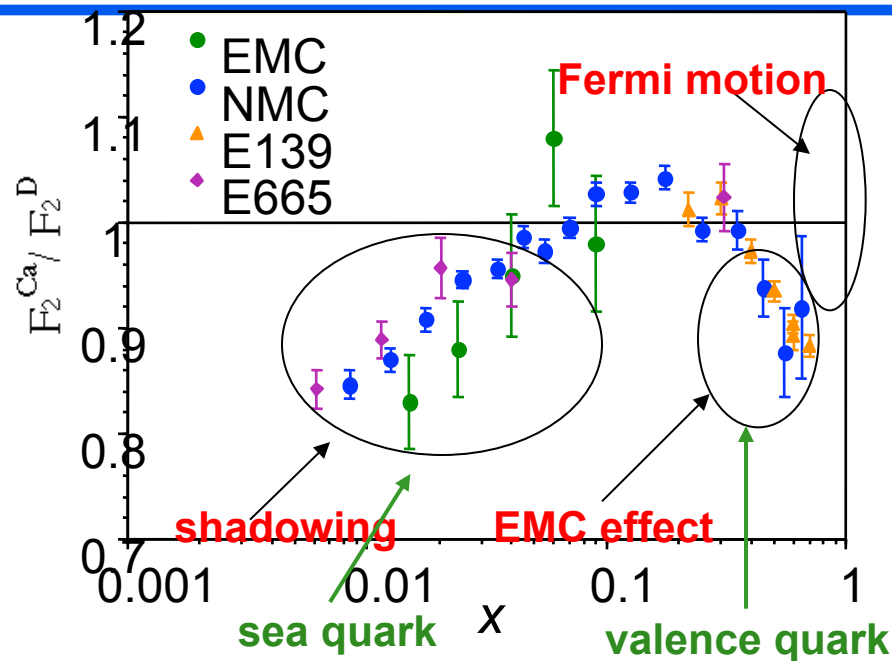
$$E_\nu = \frac{2M_N E_\mu - m_\mu^2}{2(M_N - E_\mu + p_\mu \cos \theta_\mu)}$$

Since all modern experiments contain nuclei as targets.

Reconstructed energy shifted to lower energies for all processes other than true QE

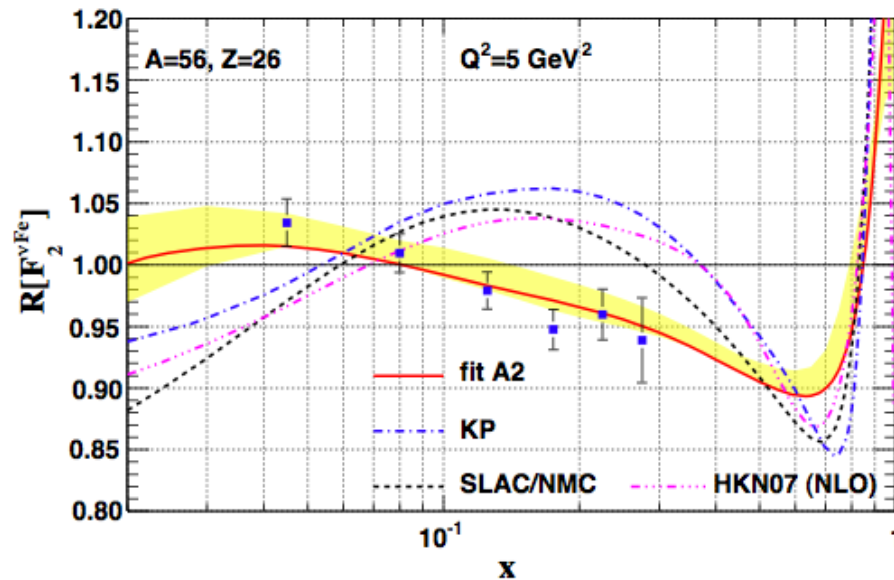


Experimental Studies of (Parton-level) Nuclear Effects with Neutrinos: until recently - essentially NON-EXISTENT



- ◆ F_2 / nucleon changes as a function of A . Specifically measured in $\mu/e - A$ **not in $\nu - A$**
- ◆ **Good reason to consider nuclear effects are DIFFERENT in $\nu - A$.**
 - ▼ Presence of axial-vector current.
 - ▼ SPECULATION: Stronger shadowing for $\nu - A$ but somewhat weaker “EMC” effect.
 - ▼ Different nuclear effects for valence and sea --> different shadowing for xF_3 compared to F_2 .

F_2 Structure Function Ratios: ν -Iron nCTEQ Collaboration



$$\frac{F_2(\nu + \text{Fe})}{F_2(\nu + [n+p])}$$

